## Letter

## Bit Storage by 360° Domain Walls in Ferromagnetic Nanorings

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We propose a theoretical design for a magnetic memory cell, based on thin-film ferromagnetic nanorings, that can efficiently store, record, and read out information. An information bit is represented by the polarity of a stable 360° domain wall introduced into the ring. Switching between the two magnetization states is done by a current applied to a wire passing through the ring, whereby the 360° domain wall splits into two charged 180° walls, which then move to the opposite extreme of the ring to recombine into a 360° wall of the opposite polarity.

Index Terms—Current-induced switching, ferromagnetic rings, magnetoresistive random access memory (MRAM), micromagnetic modeling, topological domain walls.

AGNETORESISTIVE random access memory (MRAM) has long been considered one of the main contenders to replace the current semiconductor-based devices as a universal, nonvolatile computer memory [1]–[4]. Nevertheless, despite recent developments of commercially available products [1], MRAM technology has yet to deliver a device that would truly compete with the existing semiconductor technologies.

In the current MRAM cell designs, the storage element is a sandwich structure which contains two ferromagnetic layers separated by a thin tunneling layer; the magnetization is fixed in one of the ferromagnetic layers, but is free to move in the other [1], [3]. The bit of information is encoded as a monodomain magnetization state of the free ferromagnetic layer which can be switched as a whole by the magnetic field generated by the current passing through the "write" lines. Readout is achieved by measuring the tunnel current through the storage element, which depends on the magnetization state. The main difficulty in designing an MRAM cell is to be able to reliably write bits of information to a specified cell. One important issue is the problem of 1/2-bit select due to the close proximity of the "write" lines to the free magnetic layer in the cross-point addressing scheme [1]. Another issue is the need to use rather strong currents to generate the magnetic fields required for switching, which makes these devices quite power-hungry.

Recently, a growing interest was attracted by a new MRAM cell design concept in which the storage element is made in the shape of a submicron-sized ring [5]–[19]. As was proposed in [5], the bit may be encoded by the direction of the vortex magnetization state in a ferromagnetic thin-film ring. A difficulty associated with this design has to do with switching between

Manuscript received January 21, 2009; revised March 12, 2009. Current version published July 22, 2009. Corresponding author: C. B. Muratov (e-mail: muratov@njit.edu).

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Digital Object Identifier 10.1109/TMAG.2009.2020329



Fig. 1. Schematics of the proposed design.

the two vortex states, since it requires creating magnetization poles at the ring boundaries. Hence, a rather elaborate writing scheme using paired word lines [5] or the use of spin-polarized current [6], [20]–[23] were called for. Note that in the latter case the current densities required to affect the magnetization state are found to be quite high (exceeding  $10^8$  A/cm<sup>2</sup>) [16], [21], [23]. Another proposal has been to pass a current of variable polarity vertically through the sandwich structure, so that the resulting circular magnetic field favors a particular orientation of the vortex or the asymmetric "onion" magnetization state [7], [13].

Here, we propose a new principle for the design of a robust MRAM cell based on thin-film ferromagnetic nanorings (see Fig. 1 for schematics). In contrast to similar previous designs [7], [24], which are based on twisted onion states (see, e.g., [7, Fig. 2b,c]), we propose to use the polarity of the tightly localized 360° domain wall (see Fig. 2) in the free ferromagnetic layer to encode the bit of information. Existence and stability of such domain walls for certain ranges of parameters was recently demonstrated by us via micromagnetic modeling and simulations [25]. Winding domain walls, including 360° walls, are

in the film plane and an easy direction



Fig. 2. Bit-encoding magnetization state with a  $-360^{\circ}$  wall on the left. The other bit is encoded by the mirror image of this magnetization pattern, with the  $+360^{\circ}$  wall on the right, respectively. From the numerical solution of (3), see the text for details.

also frequently observed experimentally in cobalt nanorings [9], [10], [12]. We further propose to use the circular field generated by a wire passing through the ring to switch between the two polarities of the  $360^{\circ}$  wall. In addition, we suggest to use a material with a moderate fourfold anisotropy to further stabilize the wall.

The basic idea of the proposed design is that in the presence of a 360° wall the magnetization pattern looks like a vortex state in most of the ring, except a small region where the wall is localized (see Fig. 2). Nevertheless, in contrast to the vortex states, its topological degree (i.e., the winding number of the magnetization vector along a closed loop traced counterclockwise inside the ring) is zero, since inside the wall the magnetization rotates in the direction opposite to the direction of rotation in the rest of the ring (for vortex states the topological degree is +1). Thus, both states corresponding to the  $\pm 360^{\circ}$  walls are accessible by smooth in-plane rotation of the magnetization vector from the "onion" state [2], [6], [8], [16], the native magnetization state in the ring following saturation by an in-plane field. Switching between these states can be achieved by passing a current of variable polarity through a wire running perpendicularly to the ring plane through its center, generating a circular magnetic field in the ring, and readout can be performed, as in previous designs, by arranging the ferromagnetic nanoring to be part of a magnetic tunnel junction sandwich, with fixed ferromagnetic ring layer in a vortex state. Note that this design is free from the 1/2-select problem, as was already pointed out in [7].

Let us demonstrate the feasibility of the proposed design by a micromagnetic study of the Landau–Lifshitz–Gilbert equation [4] for the magnetization vector  $\mathbf{M} = \mathbf{M}(\mathbf{r}, t)$  in the ferromagnetic ring (denoted by  $\Omega \subset \mathbb{R}^3$ )

$$\frac{\partial \mathbf{M}}{\partial t} = -\frac{g|e|}{2mc} \left( \mathbf{M} \times \mathbf{H}_{\text{eff}} + \frac{\alpha}{M_s} \mathbf{M} \times \mathbf{M} \times \mathbf{H}_{\text{eff}} \right) \quad (1)$$

with Neumann boundary condition on the material boundary  $\partial\Omega$ . The effective field  $\mathbf{H}_{\text{eff}} = -\delta E/\delta \mathbf{M}$ , with

$$E[\mathbf{M}] = \int_{\Omega} \left( \frac{K}{2M_s^4} M_1^2 M_2^2 + \frac{A}{2M_s^2} |\nabla \mathbf{M}|^2 - \mathbf{H} \cdot \mathbf{M} \right) d^3 \mathbf{r} + \frac{1}{2} \int_{\mathbb{R}^3} \int_{\mathbb{R}^3} \frac{\nabla \cdot \mathbf{M}(\mathbf{r}) \nabla \cdot \mathbf{M}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d^3 \mathbf{r} d^3 \mathbf{r}'.$$
(2)

$$\theta_t = \Delta \theta - \frac{1}{4} \sin 4\theta - h_1 \cos \theta - h_2 \sin \theta + \nu \varphi_x \cos \theta + \nu \varphi_y \sin \theta$$
(3)  
$$\varphi = \frac{1}{2} (-\Delta)^{-1/2} (\theta_x \cos \theta + \theta_y \sin \theta) + \text{boundary terms}$$
(4)

where lengths were rescaled by  $L = (A/K)^{1/2}$ , and the thin-film parameter  $\nu = d/(lQ^{1/2})$  was introduced [27], where  $l = (A/4\pi M_s^2)^{1/2}$  is the exchange length and  $Q = K/(4\pi M_s^2)$  is the material's quality factor.

We now investigate the process of switching in a ferromagnetic nanoring by performing a numerical simulation of (3) in a ring of diameter 30 and width 5, with  $\nu = 10$ , and  $h_1 =$  $\mp 3.2y/(x^2 + y^2), h_2 = \pm 3.2x/(x^2 + y^2), \text{ or } h_{1,2} = 0, \text{ de-}$ pending on the current through the central wire (all quantities are dimensionless, see the following paragraph for a physical interpretation; the details of the numerical method are as in [25]). At t = 0, the magnetization is saturated by a field along the y-axis. As the field is removed, the magnetization settles into the symmetric onion state (Fig. 3, t = 20). Then, a positive current is applied through the wire, generating a counterclockwise magnetic field, which drives the poles of the onion and the associated charged 180° walls towards each other on the left side of the ring. At  $t \simeq 100$  these two walls collide to form a 360° wall (Fig. 3, t = 120). Importantly, when the current is stopped, the resulting 360° wall maintains its integrity and does not break up (Fig. 3, t = 160, same as Fig. 2, consistently with our earlier studies of 360° walls [25]). Applying a negative current leads, in turn, to a breakup of the 360° wall. The resulting charged 180° walls propagate along the ring to collide at the opposite extreme on the right and form a new 360° wall of opposite polarity (Fig. 3, t = 320). As before, when the current is switched off, the wall remains in its place (not shown). Note that no magnetic poles need to be created during switching, the existing poles simply move back and forth along the ring boundaries.

In conclusion, we have demonstrated the feasibility of storage and writing of a bit in the form of  $\pm 360^{\circ}$  walls in a thin-film ferromagnetic ring. The dimensionless parameters used in the simulation can be translated, e.g., to those of a cobalt (l = 3.37 nm,  $M_s = 1400 \text{ emu/cm}^3$ , Q = 0.08 [6], [26]) ring of diameter 350 nm, width 60 nm, and thickness d = 9.6 nm. The current producing the required circular magnetic field is J = 27 mA, corresponding to a moderate current density of  $6 \times 10^7$  A/cm<sup>2</sup>. Note that a way to further reduce the switching current density is to use a softer material (with smaller Q and d), at the expense of increasing the ring diameter. We emphasize that this design is expected to be very robust, in view of the stability of the underlying 360° walls [25] and the topologically constrained switching process. Finally, note that the proposed cell geometry allows to stack the rings vertically by interrupting the vertical wire with horizontal lines of alternating directions, suggesting a possibility to greatly increase the memory capacity by harnessing the third dimension.



Fig. 3. Dynamics of the magnetization reversal in a ferromagnetic nanoring subject to the magnetic field from a wire passing through the ring center. Results of the numerical simulations of (3) (see text for details).

## ACKNOWLEDGMENT

The work of the first author was supported in part by the National Science Foundation under Grant DMS-0718027.

## References

- J. Åkerman, "Toward a universal memory," *Science*, vol. 308, pp. 508–510, 2005.
- [2] C. L. Dennis, R. P. Borges, L. D. Buda, U. Ebels, J. F. Gregg, M. Hehn, E. Jouguelet, K. Ounadjela, I. Petej, I. L. Prejbeanu, and M. J. Thornton, "The defining length scales of mesomagnetism: A review," *J. Phys Condens. Mater.*, vol. 14, pp. R1175–R1262, 2002.
- [3] S. Tehrani, J. M. Slaughter, M. Deherrera, B. N. Engel, N. D. Rizzo, J. Salter, M. Durlam, R. W. Dave, J. Janesky, B. Butcher, K. Smith, and G. Grynkewich, "Magnetoresistive random access memory using magnetic tunnel junctions," *Proc. IEEE*, vol. 91, no. 5, pp. 703–714, May 2003.
- [4] A. Hubert and R. Schäfer, *Magnetic Domains*. Berlin, Germany: Springer, 1998.
- [5] J.-G. Zhu, Y. Zheng, and G. A. Prinz, "Ultrahigh density vertical magnetoresistive random access memory (invited)," *J. Appl. Phys.*, vol. 87, pp. 6668–6673, 2000.
- [6] S. P. Li, D. Peyrade, M. Natali, A. Lebib, Y. Chen, U. Ebels, L. D. Buda, and K. Ounadjela, "Flux closure structures in cobalt rings," *Phys. Rev. Lett.*, vol. 86, pp. 1102–1105, Feb. 2001.
- [7] X. Zhu and J.-G. Zhu, "A vertical MRAM free of write disturbance," *IEEE Trans. Magn.*, vol. 39, no. 5, pp. 2854–2856, Sep. 2003.
- [8] M. Kläui, C. A. F. Vaz, L. Lopez-Diaz, and J. A. C. Bland, "Vortex formation in narrow ferromagnetic rings," J. Phys. Condens. Mater., vol. 15, pp. R985–R1024, 2003.
- [9] F. J. Castaño, C. A. Ross, C. Frandsen, A. Eilez, D. Gil, H. I. Smith, M. Redjdal, and F. B. Humphrey, "Metastable states in magnetic nanorings," *Phys. Rev. B*, vol. 67, p. 184425, 2003.
- [10] F. J. Castaño, C. A. Ross, A. Eilez, W. Jung, and C. Frandsen, "Magnetic configurations in 160–520 nm-diameter ferromagnetic rings," *Phys. Rev. B*, vol. 69, p. 144421, 2004.
- [11] T. J. Hayward, J. Llandro, R. B. Balsod, J. A. C. Bland, F. J. Castaño, D. Morecroft, and C. A. Ross, "Reading and writing of vortex circulation in pseudo-spin-valve ring devices," *Appl. Phys. Lett.*, vol. 89, p. 112510, 2006.
- [12] C. A. Ross, F. J. Castaño, D. Morecroft, W. Jung, H. I. Smith, T. A. Moore, T. J. Hayward, J. A. C. Bland, T. J. Bromwich, and A. K. Petford-Long, "Mesoscopic thin-film magnetic rings (invited)," *J. Appl. Phys.*, vol. 99, p. 08S501, 2006.
- [13] M. T. Moneck and J.-G. Zhu, "Fabrication and testing of deep submicron annular vertical magnetoresistive random access memory elements," J. Appl. Phys., vol. 99, p. 08H709, 2006.

- [14] F. Q. Zhu, G. W. Chern, O. Tchernyshyov, X. C. Zhu, J. G. Zhu, and C. L. Chien, "Magnetic bistability and controllable reversal of asymmetric ferromagnetic nanorings," *Phys. Rev. Lett.*, vol. 96, p. 027205, 2006.
- [15] K. Martens, D. L. Stein, and A. D. Kent, "Magnetic reversal in nanoscopic ferromagnetic rings," *Phys. Rev. B*, vol. 73, p. 054413, 2006.
- [16] C. A. F. Vaz, T. J. Hayward, J. Llandro, F. Schackert, D. Morecroft, J. A. C. Bland, M. Kläui, M. Laufenberg, D. Backes, U. Rudiger, F. J. Castano, C. A. Ross, L. J. Heyderman, F. Nolting, A. Locatelli, G. Faini, S. Cherifi, and W. Wernsdorfer, "Ferromagnetic nanorings," J. *Phys. Condens. Mater.*, vol. 19, p. 255207, 2007.
- [17] N. Benatmane, W. Scholz, and T. W. Clinton, "Magnetic configurations and phase diagrams of sub-100-nm NiFe nanorings," *IEEE Trans. Magn.*, vol. 43, no. 6, pp. 2884–2886, Jun. 2007.
- [18] X. F. Han, Z. C. Wen, and H. X. Wei, "Nanoring magnetic tunnel junction and its application in magnetic random access memory demo devices with spin-polarized current switching (invited)," J. Appl. Phys., vol. 103, p. 07E933, 2008.
- [19] A. O. Adeyeye, S. Goolaup, N. Singh, W. Jun, C. C. Wang, S. Jain, and D. Tripathy, "Reversal mechanisms in ferromagnetic nanostructures," *IEEE Trans. Magn.*, vol. 44, no. 7, pp. 1935–1940, Jul. 2008.
- [20] M. Tsoi, A. G. M. Jansen, J. Bass, W.-C. Chiang, M. Seck, V. Tsoi, and P. Wyder, "Excitation of a magnetic multilayer by an electric current," *Phys. Rev. Lett.*, vol. 80, pp. 4281–4284, 1998.
- [21] E. B. Myers, D. C. Ralph, J. A. Katine, R. N. Louie, and R. A. Buhrman, "Current-induced switching of domains in magnetic multilayer devices," *Science*, vol. 285, pp. 867–870, Aug. 1999.
- [22] J. Bass, S. Urazhdin, N. O. Birge, and W. P. Pratt, "Current-driven excitations in magnetic multilayers: A brief review," *Phys. Stat. Sol. A*, vol. 201, pp. 1379–1385, 2004.
- [23] M. Klaui, C. A. F. Vaz, J. A. C. Bland, W. Wernsdorfer, G. Faini, E. Cambril, L. J. Heyderman, F. Nolting, and U. Rudiger, "Controlled and reproducible domain wall displacement by current pulses injected into ferromagnetic ring structures," *Phys. Rev. Lett.*, vol. 94, p. 106601, 2005.
- [24] C. A. Ross and F. J. Castano, "Magnetic Memory Elements Using 360 ° Walls," U.S. Patent 6 906 369 B2, 2005.
  [25] C. B. Muratov and V. V. Osipov, "Theory of 360 ° domain walls in
- [25] C. B. Muratov and V. V. Osipov, "Theory of 360 ° domain walls in thin ferromagnetic films," J. Appl. Phys., vol. 104, pp. 053908-1–14, 2008.
- [26] B. Heinrich and J. F. Cochran, "Ultrathin metallic magnetic films: Magnetic anisotropies and exchange interactions," *Adv. Phys.*, vol. 42, pp. 523–639, 1993.
- [27] C. B. Muratov and V. V. Osipov, "Optimal grid-based methods for thin film micromagnetics simulations," J. Comput. Phys., vol. 216, pp. 637–653, 2006.