

PROPRIETA'

(I)  $A$  e' a PDF  $\Rightarrow A[k]$  e' a PDF per  $k=1, \dots, n$

(II)  $A$  e' a PDF  $\Rightarrow \det A \neq 0$

(dim: (I) ovvio dalla def; (II) si dim che PDF  $\Rightarrow \ker A = \{0\} \dots$ )

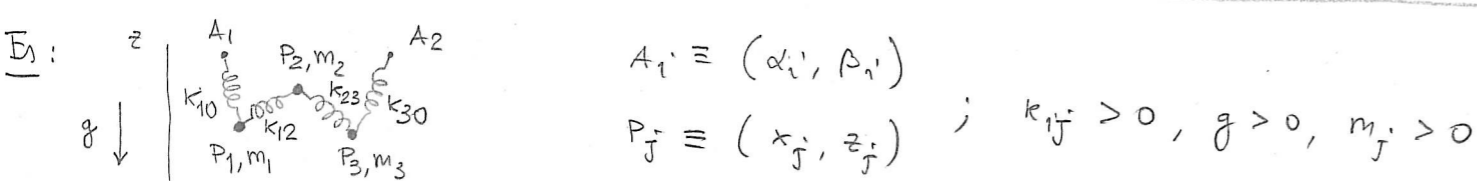
Allora: (I) + (II):  $A$  e' a PDF  $\Rightarrow \det A[k] \neq 0, k=1, \dots, n-1$   
 q.d' (tes ris def EG): EG e' def in  $A$ .

② SDP def:  $A \in \mathbb{R}^{n \times n}$  e' SDP se  $\begin{cases} A \text{ e' simm (} A^T = A \text{)} \\ \forall v \neq 0, Av \cdot v > 0 \\ \text{(ps canonico in } \mathbb{R}^n \text{)} \end{cases}$

Es:  $\alpha I \in \mathbb{R}^{n \times n}, \alpha \in \mathbb{R}$ , e' simm  $\forall \alpha$ ;  $v^T \alpha v = \alpha \|v\|^2$ ;  
 $\alpha I$  e' SDP  $\Leftrightarrow \alpha > 0$  (ris gen: diag  $(\alpha_1, \dots, \alpha_n)$  e'  
 SDP  $\Leftrightarrow \alpha_i > 0, \dots, \alpha_n > 0$ )

$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \in \mathbb{R}^{2 \times 2}$  e' simm;  $v^T \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} v = 2v_1 v_2$  e q.d' ... non e' SDP.

Oss:  $A e_k \cdot e_k = e_k^T A e_k = a_{kk}$ , percio':  $A$  SDP  $\Rightarrow a_{kk} > 0, k=1, \dots, n$ .



Eq per l'equilibrio (eq di Newton):

$$\underbrace{\begin{bmatrix} k_{10} + k_{12} & -k_{12} & 0 \\ -k_{12} & k_{12} + k_{23} & -k_{23} \\ 0 & -k_{23} & k_{23} + k_{30} \end{bmatrix}}_{C \in \mathbb{R}^{3 \times 3}} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} k_{10} \alpha_1 \\ 0 \\ k_{30} \alpha_2 \end{bmatrix} \quad \text{proiez lungo asse } x$$

$$C \begin{bmatrix} z_1 \\ z_2 \\ z_3 \end{bmatrix} = \begin{bmatrix} k_{10} \beta_1 - m_1 g \\ -m_2 g \\ k_{30} \beta_2 - m_3 g \end{bmatrix} \quad \text{proiez lungo asse } z$$

Oss: i' due sistemi hanno la stessa matrice.

...  $C$  e' SDP (vero sempre per sist di masse e molle)

(dim: dalla def:  $Cv \cdot v = \dots$ )

PROPRIETA'

(I)  $A$  e' SDP  $\Rightarrow A[k]$  e' SDP,  $k=1, \dots, n$

(II)  $A$  e' SDP  $\Rightarrow \det A \neq 0$

(dim: (I) no, (II)  $Ax=0 \Rightarrow Ax \cdot x = 0 \dots$ )

Allora: (I) + (II)  $A$  e' SDP  $\Rightarrow \det A[k] \neq 0$  per  $k=1, \dots, n-1$   
 q.d' (tes ris def EG): EG e' def in  $A$

Oss:

